Operating manual and detailed algorithms for conducting stochastic future projections with R packages of 'ssfuture'

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1 Introduction

Stock Synthesis (SS) is currently one of the most commonly used software for stock assessment. The software provides statistical framework for calibration of a population dynamics model using a diversity of fishery and survey data (Methot, 2005). SS can also provide outlooks for future population dynamics with deterministic projections from the estimated parameters during the stock assessment period. In the future projection phase, SS provide averages of future statistics such as spawning biomass (SSB) and standard deviations of the future statistics. The standard deviations are estimated by Hessian-matrix under normal approximation (Maunder et al., 2006) or by MCMC. Therefore, the estimated future statistics (such as future SSB) in SS are assumed to distribute normally, and not reflect future stochastic uncertainty.

On the other hand, stochastic future projections are sometimes important for evaluating current stock status and future management procedures. Simulation-based reference points of F_{ssb} (Conser et al. 2006; Ichinokawa et al., 2010) are used as an interim reference point for this stock for North Pacific albacore stock. Future stochastic projections for the stock assessment of Pacific bluefin tuna in ISC have been conducted with specific software coded by R (cf. Ichinokawa et al., 2008). Suites of reference points are also produced with this software (cf. Kai et al. 2010).

This appendix made detailed description on algorithms to conduct stochastic future projections and reference points from outputs by Stock Synthesis with the R-code.

2 Population dynamics

2.1 Definition of parameters and dimension for population dynamics

Table 1 shows definition of parameters used in this document. Basically, parameters estimated during the stock assessment phase are expressed by lower cases; those during future projection phase are by upper cases. For example, numbers at age a ($0 \leq a \leq Amax$) and time t at the bth bootstrap run during the stock assessment period is expressed as $n^{b}_{a,t}$, while those in the future projection period are expressed by $N^{b,k}_{a,t}$. The superscript of b, representing the bth bootstrap results, can range from 0 to the number of bootstrap iterations of X_b. The 0th iteration represents maximum likelihood estimation.

Since multiple season per year can be assumed in SS, estimated parameters in SS include the dimension of season ($0 \leq s \leq nseason$). However, because description of the additional dimension make the R-code complicated, population dynamics used in the future projections didn't include the dimension of season. Instead, the time series is expanded by year and season to use year interval of $i = 1/nseason$. For example, time series from 1952 to 2006 with 4 seasons can be expressed by $t = 1952, 1952.25, 1952.5, ..., 2005.5, 2005.75$, and age classes from 0 to 20 years old are by $a = 0, 0.25, 0.5, ..., 19.5, 19.75$. Then, estimates in SS of $n_{a,s,t}$ (numbers at age at the beginning of the

Table 1: Parameters used in this document

Parameter	Description
$n^b_{a,t}$, $N^{k,b}_{a,t}$	Population numbers at beginning of season
$f^b_{a,t}$, $F^{k,b}_{a,t}$	Instantaneous rate of fishing mortality during the stock assessment period (lower case) and future projection period (upper case)
$c^b_{a,t}$, $C^{k,b}_{a,t}$	Catch at age during the stock assessment period (lower case) and future projection period (upper case)
M_a	Instantaneous rate of natural mortality (/yr)
w_a	Weight at age at the beginning of season
w_{af}	Weight at age by fleet at the beginning of season
Q_a	Maturity rates at age
Fcur_a	Current F, which is produced by averaging a current F period
PFcur_{af}	Partial F corresponding with Fcur_a. $\sum_{k=1}^{nfleet} \mathrm{PFcur}_{af} = \mathrm{Fcur} = a$
b^b_t,B^b_t	Stock biomass at the beginning of the year
ssb^b_t,SSB^b_t	SSB spawning stock biomass at the beginning of the spawning season
PTC^b_t,TC^b_t	Total catch by fleet, and total catch in weight
t_1, t_2	Generic parameters specifying a range of time period from t_1 to t_2 (Table 2)
$nseason$	Number of seasons per year (inherited from SS)
$nfleet$	Number of fisheries (inherited from SS)
i	Time interval = 1/qt
A_{min},A_{max}	Minimum and maximum age considered in the stock assessment model and future projection. Plus groups are included in the age of A_{max}. Recruitments are assumed to occur at $a = 0$.
X_s	Number of stochastic simulations. $k = 1, 2, ..., X_s$.
X_b	Number of bootstrap iterations. $b = 0, 1, 2, ..., X_s$. The 0th iteration represents point estimates.

time time interval t),$c_{a,s,t}$ (catch at age of age a during the time interval t), and $c_{a,s,t,f}$ (partial catch at age by fisheries) are rewritten as the following equations.

$$n_{a+(s-1)/qt,t+(s-1)/qt} = \begin{cases} n_{a,s,t} & \text{if} \quad n_{a,s,t} > 0 \\ \mathrm{NA} & \text{if} \quad n_{a,s,t} = 0 \end{cases} \tag{1}$$

$$c_{a+(s-1)/qt,t+(s-1)/qt} = \begin{cases} c_{a,s,t} & \text{if} \quad n_{a,s,t} > 0 \quad and \quad a < A_{max} \\ \frac{1}{nseason} \sum_{s=1}^{nseason} c_{a,s,t} & \text{if} \quad n_{a,s,t} > 0 \quad and \quad a = A_{max} \\ \mathrm{NA} & \text{if} \quad n_{a,s,t} = 0 \end{cases} \tag{2}$$

$$c_{a+(s-1)/qt,t+(s-1)/qt,f} = \begin{cases} c_{a,s,t,f} & \text{if} \quad n_{a,s,t,f} > 0 \quad and \quad a < A_{max} \\ \frac{1}{nseason} \sum_{s=1}^{nseason} c_{a,s,t,f} & \text{if} \quad n_{a,s,t} > 0 \quad and \quad a = A_{max} \\ \mathrm{NA} & \text{if} \quad n_{a,s,t} = 0 \end{cases} \tag{3}$$

'NA' stands for a blank element, where corresponding population does not exist. Also, since all elements of $n_{a,t}, c_{a,t}, c_{a,t,f}$ can't be filled with the above equation, remaining elements are filled by 'NA'. Those blank columns expressed by 'NA' are ignored int the following calculations. Note that, in the case of catch at age, catch of terminal ages are assumed to be an average through the season.

2.2 Current F

Current F (Fcur_a) is defined from the parameters estimated in the stock assessment period, numbers at age ($n^b_{a,t}$) and catch at age ($c^b_{a,t}$). First, $f^b_{a,t}$ is estimated by solving the following catch equation.

$$c^b_{a,t} = \frac{f_{a,t}}{f_{a,t} + M_a}(1 - \exp(-f_{a,t} - M_a))n_{a,t} \tag{4}$$

Given the time range representative to 'current' as $t_1 \leq t < t_2$, the current F of Fcur_a is calculated by averaging F at age during the time range. In averaging F at age through the current F period, two options can be selected: simple or geometric average. In using simple average, the following equation is used.

$$\text{Fcur}_a = \frac{1}{\text{number of years}} \sum^{t_1 \leq t < t_2} f_{a,t} \tag{5}$$

Otherwise, geometric mean can also be available.

$$\text{Fcur}_a = \exp\left(\sum^{t_1 \leq t \leq t_2} \log f_{a,t} \frac{1}{\text{number of years}}\right) \tag{6}$$

Current F by fleet ($\text{Fcur}_{a,f}$) is also calculated as following equations using partial catch at age ($c_{a,t,f}$).

$$\text{Fcur}_{a,f} = \text{Fcur}_a \text{PFcur}_{a,f} \tag{7}$$

where

$$\text{PFcur}_{a,f} = \frac{1}{\text{number of years}} \sum^{t_1 \leq t \leq t_1} \frac{c_{a,t,f}}{c_{a,t}} \tag{8}$$

The parameter of $\text{PFcur}_{a,f}$ is partial catch ratio assumed in the current F, which is utilized in calculating partial catch in weight by fleet in future. Note that the $\text{PFcur}_{a,f}$ is calculated by using simple average, even though the option of 'geometric mean' is used. This is because zero partial fishing mortality appears frequently, which cause inability to calculate geometric mean.

2.3 Population dynamics in future

Numbers at age $N^{k,b}_{a,y}$ in the future period ($t_1 \leq t \leq t_2$) are calculated as the following equations.

$$N^{k,b}_{a,t_1} = \begin{cases} R^{k,b}_t & a = 0 \quad \text{and} \quad t = \text{recruitment timing} \\ 0 & a = 0 \quad \text{and} \quad t \neq \text{recruitment timing} \\ n^b_{a,t_1} & \end{cases} \tag{9}$$

$$N^{k,b}_{a,t} = \begin{cases} R^{k,b}_t & a = 0 \quad \text{and} \quad t = \text{recruitment timing} \\ 0 & a = 0 \quad \text{and} \quad t \neq \text{recruitment timing} \\ N^{k,b}_{a-i,t-i} \exp(-F_{a-i} + -M_{a-i}) & 0 < a < A_{max} \\ N^{k,b}_{a-i,t-i} \exp(-F_{a-i} + -M_{a-i}) + N^{k,b}_{a,t-i} \exp(-F_a + -M_a) & a = A_{max} \end{cases} \tag{10}$$

Future recruitment of R_t and fishing mortality at age of F_a are determined by optional scenarios of recruitment (see section 3) and harvesting (see section 4).

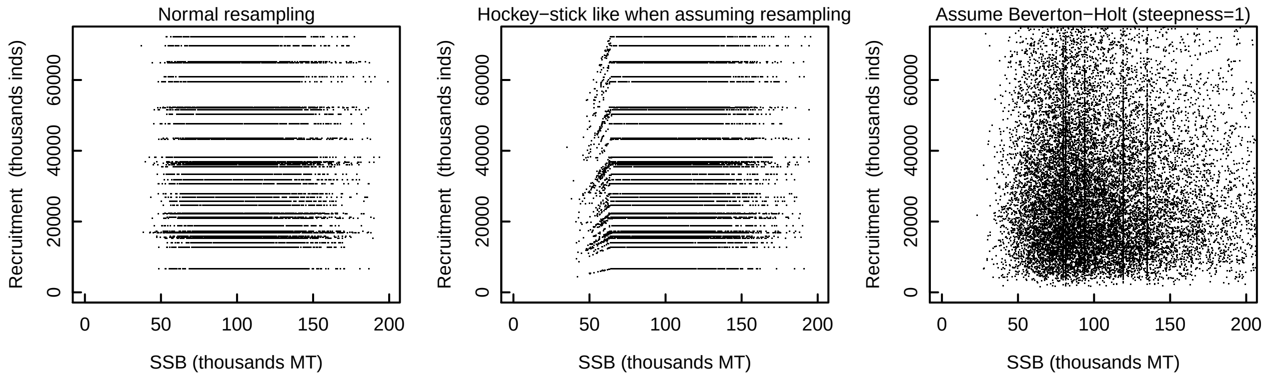

Figure 1: Examples of future recruitment scenarios. Left panel: simple re-sampling of past recruitments during 1965−2008. Middle panel: assuming hockey-stick type recruitments based on re-sampling of past recruitments. In this example, the threshold of SSB is set to be lower 20% of the historically observed SSB. Right panel: beverton-Holt spawner-recruitment relationship and log-normal error. Parameters of the S-R curve are inherited from the estimates in SS. In this example, steepness is fixed as 1 in SS.

Future statistics of total biomass ($B_t^{k,b}$) and SSB ($\mathrm{SSB}_t^{k,b}$) are calculated.

$$B_y^{k,b} = \sum_{a=0}^{A_{max}} w_a N_{a,t}^{k,b} \tag{11}$$

$$\mathrm{SSB}_y^{k,b} = \sum_{a=0}^{A_{max}} w_a Q_a N_{a,t}^{k,b} \tag{12}$$

weight at age, w_a, is derived from SS results (column specified by 'Wt_Beg'). Total catch ($\mathrm{TC}_t^{k,b}$, in weight) and total partial catch by fisheries ($\mathrm{PTC}_t^{k,b}$, in weight) are also calculated.

$$\mathrm{TC}_t^{k,b} = \sum_{f=1}^{nfleet} \mathrm{PTC}_{t,f}^{k,b} = \sum_{f=1}^{nfleet} w_{a,f} \sum_{a=0}^{A_{max}} \frac{F_a \mathrm{PFcur}_{a,f}}{F_a + M_a} (1 - exp(-F_a + M_a)) N_{a,t}^{k,b} \tag{13}$$

Fishery specific weight at age (w_{af}) is used in calculating TC and PTC. The parameter of w_{af} is derived from SS results (column specified by 'Selwt' in Report.sso).

3 Recruitment scenarios

Following scenarios are available for future recruitments.

3.1 Simple resampling (REC.resample)

This scenario assumes future recruitments as random re-samplings from recruitments estimated in the stock assessment periods specified by $t_1 \leq t \leq t_2$.

$$R_t^{k,b} = \begin{cases} \text{random draw from} \quad n_{0,t_1 \leq t \leq t_2} & t = \text{recruitment timing} \\ 0 & t \neq \text{recruitment timing} \end{cases} \tag{14}$$

Followings are required configurations in using this recruitment scenario.

REC.resample	
year.lim(=NULL)	Give a vector with 2 elements of t_1 and t_2
qt(=1)	Assumed number of seasons per year (be consistent with SS configuration).
recruit.qt(=1)	Season when recruitments occur (be consistent with SS configuration). Currently, multiple recruitments per year can't be assumed with this R-code.

3.2 Beverton-Holt S-R relation + stochastic error (REC.beverton.ss)

Future recruitment is assumed to occur according to the Beverton-Holt relationship with stochastic error of random lognormal or random resampling of past deviances of recruitment *logRdev* during a certain year range specified by year.lim ($t_1 \le t \le t_2$). The parameters of the stock-recruitment relationship (h, S_0, R_0) and σR is basically derived from SS output.

If option of resample=FALSE,

$$R_t^{k,b} = \begin{cases} \hat{R}_t \exp\left(N(-\sigma^2/2, \sigma^2)\right) & t = \text{recruitment timing} \\ 0 & t \neq \text{recruitment timing} \end{cases} \tag{15}$$

(16)

If option of resample=TRUE,

$$R_t^{k,b} = \begin{cases} \hat{R}_t \exp\left(-\sigma^2/2 + \text{random draw from} \quad logRdev_{t_1 \le t \le t_2}\right) & t = \text{recruitment timing} \\ 0 & t \neq \text{recruitment timing} \end{cases} \tag{17}$$

where

$$\hat{R}_t = \frac{4hR_0\mathrm{SSB}_t}{S_0(1-h) + \mathrm{SSB}_t(5h-1)} \tag{18}$$

REC.beverton.ss	
recruit.qt(=1)	Season when recruitments occur (be consistent with SS configuration). Currently, multiple recruitments per year can't be assumed with this R-code.
resampled(=FALSE)	Type of stochastic error. If resampled=TRUE, randomly resample recruitment deviation. If resampled=FALSE, random lognormal error is assumed.
year.lim(=NULL)	Give a vector with 2 elements of t_1 and t_2 when resampled=TRUE.
(steepness, R0, Rsigma, B0)	If those parameters are explicitly given, those parameters are used instead of parameters assumed in SS.

3.3 Assume empirical spawner-recruit relationship (REC.twophase)

This option is only for testing the effects of empirical spawner-recruit relationship observed in the Pacific bluefin tuna.

3.4 Options applied to all recruitment scenarios

In addition, hockey-stick type recruitments can be assumed for the all recruitment scenarios. The parameter of $\text{SSB}_{threshold}$ should be specified with this option.

$$R'_t = \begin{cases} R_t \frac{\text{SSB}_t}{\text{SSB}_{threshold}} & \text{SSB}_t \leq \text{SSB}_{threshold} \\ R_t & \text{SSB}_t > \text{SSB}_{threshold} \end{cases} \tag{19}$$

4 Harvesting scenarios

4.1 Constant F (MP.CESqt3)

F_a is given by Fcur_a scaled by a multiplier, F_{multi}, determined by the optional settings described below.

$$F_a = F_{multi} * \text{Fcur}_a \tag{20}$$

MP.CESqt3	
Fyear1(=NULL)	Give a vector with 2 elements of t_1 and t_2. The parameter of Fcur_a is calculated with this time duration. Fyear1 is used before the year to start regulation.
Fyear2(=NULL)	Give a vector with 2 elements of t_1 and t_2. The parameter of Fcur_a is calculated with this time duration. Fyear2 is used after the year to start regulation.
start.regulation(=2011)	Start year for regulation (switch F vectors from Fyear1 to Fyear2).
CES.multi(=1)	Simple multiplier to F_a (both for Fyear1 and Fyear2).
gm(=FALSE)	Use geometric mean (TRUE) or simple average (FALSE) for calculating Fcur_a.
CES.plus(=0)	Simple additional F to F_a.
CES.multi.year(=NULL)	Multiple vectors when changing multipliers to F_a by year. Even though the population dynamic consider season, this vector is given by year.
catch.capping(=NULL)	Set upper limit of annual partial catch (MT) by fleet. 'NULL' is not to use this option. If using this option, provide a list to specify target fisheries, upper limit of catch and reset timing. For example, the list is specified by 'list(reg.fleet=c(2,3),upper.catch=c(3000,1000),reset.timing=c(2,1))', which means Fleet 2 and 3 have upper limit of catch, 3000 and 1000 MT, in weight with fishing season starting 2 and 3rd quarter, respectively.
fleet.multi1(=NULL)	Multiple vectors when changing multipliers by fleet, applied to Fyear1.
fleet.multi2(=NULL)	Multiple vectors when changing multipliers by fleet, applied to Fyear2.

4.2 Constant catch by season (MP.CHSfleet)

F_a is given by $\text{Fcur}_a = \text{PFcur}_{af}$ scaled by a multiplier determined by solving catch equation (eq. 13) to archieve given future catches in weight by season.

MP.CHSfleet	
CHS.qt (=NULL)	Give a vector with *nsesaon* elements assigning catch in weight per quarter.
Fcur1(=NULL)	Give a vector with 2 elements of t_1 and t_2. The parameter of $\mathrm{Fcur}_a and \mathrm{PFcur}_{af}$ is calculated with this time duration. Fcur1 is used before the year to start regulation. In constant catch scenario, the estimated $\mathrm{Fcur}_a and \mathrm{PFcur}_{af}$ is scaled to adjust constant catch.
Fcur2(=NULL)	Give a vector with 2 elements of t_1 and t_2. The parameter of Fcur_a is calculated with this time duration. Fcur1 is used after the year to start regulation. In constant catch scenario, the estimated $\mathrm{Fcur}_a and \mathrm{PFcur}_{af}$ is scaled to adjust constant catch.
start.regulation(=2011)	Start year for regulation (switch F vectors from Fcur1 to Fcur2).
gm(=FALSE)	Use geometric mean (TRUE) or simple average (FALSE) for calculating Fcur_a.

4.3 Hybrid scenario by year (MP.hybrid)

If you want to change harvesting scenario by year, you can use this option. With this option, harvesting scenarios can be switched among years. For this scenario, MP arguments is to be 'MP.hybrid', and provide lists of mp.arguments where harvesting scemario and appied year range is specified.

4.4 Scenarios not implemented

- Constant catch by quarter and fleet

5 Calculation of reference points

5.1 F_{ssb}

F_{ssb} is based on the probability that future SSB will fall below a given threshold of $\mathrm{SSB}_{threshold}$ at one or more years, during the assumed projection period ($t_1 \leq t \leq t_2$). The probability can be calculated from results of the stochastic projections.

$$\Pr\left[\mathrm{SSB}^{k,b}_{future} < \mathrm{SSB}^{b}_{threshold}|F\right] = \frac{1}{X_b X_s}\sum_{k=1}^{X_b X_s} ||\min\left(\mathrm{SSB}^{k,b}_{t_1 \leq t \leq t_2}\right) < \mathrm{SSB}^{b}_{threshold}|| \tag{21}$$

, where the double bracket || indicates a logical test with outcome 0 (if false) or 1 (if true). Note that the probability is different from the probability that SSB at nearly equilibrium year, $\mathrm{SSB}_{equilibrium}$, falls below the $\mathrm{SSB}_{threshold}$ as follows.

$$\Pr\left[\mathrm{SSB}_{equilibrium} < \mathrm{SSB}_{threshold}|F\right] = \frac{1}{X_b X_s}\sum_{k=1}^{X_b X_s} ||\min\left(\mathrm{SSB}^{k}_{equilibrium}\right) < \mathrm{SSB}_{threshold}|| \tag{22}$$

The F-based reference point of F_{ssb} is determined by letting the probability, $Pr\left[\mathrm{SSB}_{future} < \mathrm{SSB}_{threshold}|F\right]$ be equal to a given probability, $Pr_{threshold}$. So, for the calculation of F_{ssb}, $\mathrm{SSB}_t hreshold, Pr_{threshold}$ and projection range of t_1 and t_2 should be specified.

The parameter of $\mathrm{SSB}_{threshold}$ is originally proposed to be $\min(\mathrm{ssb}_{t1 \leq t \leq t2})$, or average of ten historical lowest (ATHL) of $\mathrm{ssb}_{t1 \leq t \leq t2}$. Currently it is not determined whether the threshold level should depend on bootstrap iteration (using $\min\left(\mathrm{ssb}^{b}_{t1 \leq t \leq t2}\right)$), or not (using point estimates of $\min\left(\mathrm{ssb}^{0}_{t1 \leq t \leq t2}\right)$).

5.2 Suites of other reference points

Other reference points based on SPR and YPR are calculated from the following functions. It is noteworthy that the oldest age in estimating SPR and YPR is extended to $3A_{max}$. However, weight at age at the ages older than A_{max} is simply equal to $w_{A_{max}}, w_{A_{max},f}$.

$$N_a = \begin{cases} 1 & a = 0 \\ N_{a-i} \exp(-F_{a-i} - M_{a-i}) & a > 0 \end{cases} \tag{23}$$

$$C_a = \frac{F_a}{F_a + M_a} \left(1 - \exp\left(-F_a - M_a\right)\right) N_a \tag{24}$$

$$C_{af} = C_a \mathrm{PFcur}_{a,f} \tag{25}$$

$$\mathrm{SPR} = \sum_{a=0}^{3A_{max}} N_a w_a Q_a \tag{26}$$

$$\mathrm{YPR} = \sum_{a=1}^{3A_{max}} \sum_{f=1}^{nfleet} C_{af} w_{af} \tag{27}$$

6 Test runs for comparing SS deterministic future projection

6.1 Validation of the R-code with deterministic run of future projections by SS

Average numbers at age (Fig. 2) and partial catch by fisheries (Fig. 3) estimated from stochastic future projections implemented by the R-code are compared with those calculated by deterministic projections implemented by SS. Those runs follow the setting of run 0, except for time period of current F. This run (run 1) used F in 2008 as current F, instead of average F during 20006-2008 in the base case.

While average numbers at age (Fig. 2) are almost identical between the two results from the R-code and SS, partial catch by fisheries and estimated SSB in weight (Fig. 3) are slightly different especially in the catch by fleet 6 and SSB. The differences of the partial catch are caused by different assumptions of annual partial F by fleet between SS and this R-code. There are no clear description on the way to assume future partial F in SS, so that the R could not trace every procedures in SS. The difference in SSB is may because SS (>3.10a) calculate weight at terminal age from initial numbers at age older than the terminal age with assumption of M=0.2, but it shouln't cause the differences. Details in future projection by SS should be asked to Dr. Methot. In near future, the R-code should be modified to follow the way to calculate weight at terminal age as used in SS.

7 Practical codes for implementing future projections

7.1 Examples

In starting future projection with this package, configuration list can be created by the function of 'create.defconf'. You can get default configulation list with this function interactively as following. This function shows all available options for future MP and recruitment scenario. Then copy and paste the resultant description for specifying configuration to your editor for editing specification as you like. Wrapper function to do future projection is 'do.projection.ss'.

```
R> create.defconf()
available option of MP: (1) MP.CESqt3 (constant F, and able to
                                    set upper limit of catch by fleet)
```

```
                        (2) MP.CESqt4 (constant F, and able to set constant catch
                                                       by a specified fleet)
                        (3) MP.CHSfleet (constant quarterly catch)
                        (4) MP.CHS (prototype of MP.CHSfleet, not quarterly catch)
Please select 1-4 [default: 1]: 1
available option of R.fun: (1) REC.resample (Resampling of past recruitment)
                           (2) REC.beverton.ss (inherit Beverton-Holt S-R relation
                                                                assumed in SS)
                           (3) REC.twophase (If SSB > historical median,
                                         resample R > R[SSB > historical median])
Please select 1-4 [default: 1]: 2
# <- Copy and paste from here
config.tmp <- list(boot=c(1,300),     # specification of bootstrap from and to
                   pred.year=30,      # Projection year
                   N=20,              # N of simulations
                   record.NAA=FALSE,  # Is detailed results such as NAA produced?
                   initial.year=2008, # initial year of projection
                   ex.ssb=0,          # Below this number, the population
                                                        is considered to extinct
                   gm=TRUE,           # Calculate selectivity by geometric
                                                             or arithmetic mean
                   qt=4,              # Number of season per year
                   MP="MP.CESqt3",    # Function for future harvesting
                   args.mp=list(CES0=NULL,CES.multi=1, # Options for future harvesting
                                start.regulation=2000,
                                Fyear1=c(2004,2006),Fyear2=c(2004,2006)),
                   Rec.fun="REC.ss2",     # Function for future recruitment
                   args.R=year.lim=c(1966,2006), # Options for future recruitment
                             qt=4,recruit.qt=2),
                   HSlimit.tmp=NULL  # Is hockey-stick option used?
                                                If yes, input vectors of SSB breakpoint.
                   )  # <- Copy and paste to here
R> config.tmp <- config.tmp <- list(boot=c(1,300),
                   pred.year=30,
                   N=20,
                   record.NAA=FALSE,
                   initial.year=2008,
                   ex.ssb=0,
                   gm=TRUE,
                   qt=4,
                   MP="MP.CESqt3",
                   args.mp=list(CES0=NULL,CES.multi=1,
                                start.regulation=2000,
                                Fyear1=c(2004,2006),Fyear2=c(2004,2006)),
                   Rec.fun="REC.ss2",
                   args.R=year.lim=c(1966,2006),qt=4,recruit.qt=2),
                   HSlimit.tmp=NULL )
R> do.projection.ss(mcore=1,bootfiles=c('Report_b01.sso','Report_b02.sso'),
                    faafiles=NULL,config.list=config.tmp)
```

do.projection.ss	
mcore (=1)	Number of CPU core used for this projection for parallel computing. Library of snow and snowfall is needed if mcore¿1.
bootfiles(=NULL)	Report files (Report.sso) of SS output.
faafiles(=NULL)	R object saved by the function of ’save’. This should be return value of calFAA.ss(‘Report.sso’). If this is NULL, calFAA.ss is conducted inside this function.
config.list(=NULL)	Configuration list for specifying future projection scenario.

8 References

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Maunder, M.N., Harley, S.J., and Hampton, J. 2006. Including parameter uncertainty in forward projections of computationally intensive statistical population dynamic models. IJ 63: 969-979.

Methot, R.D., and Fisheries, N. 2005. Technical description of the Stock Synthesis II assessment program. Version 1.17. Seattle, WA.

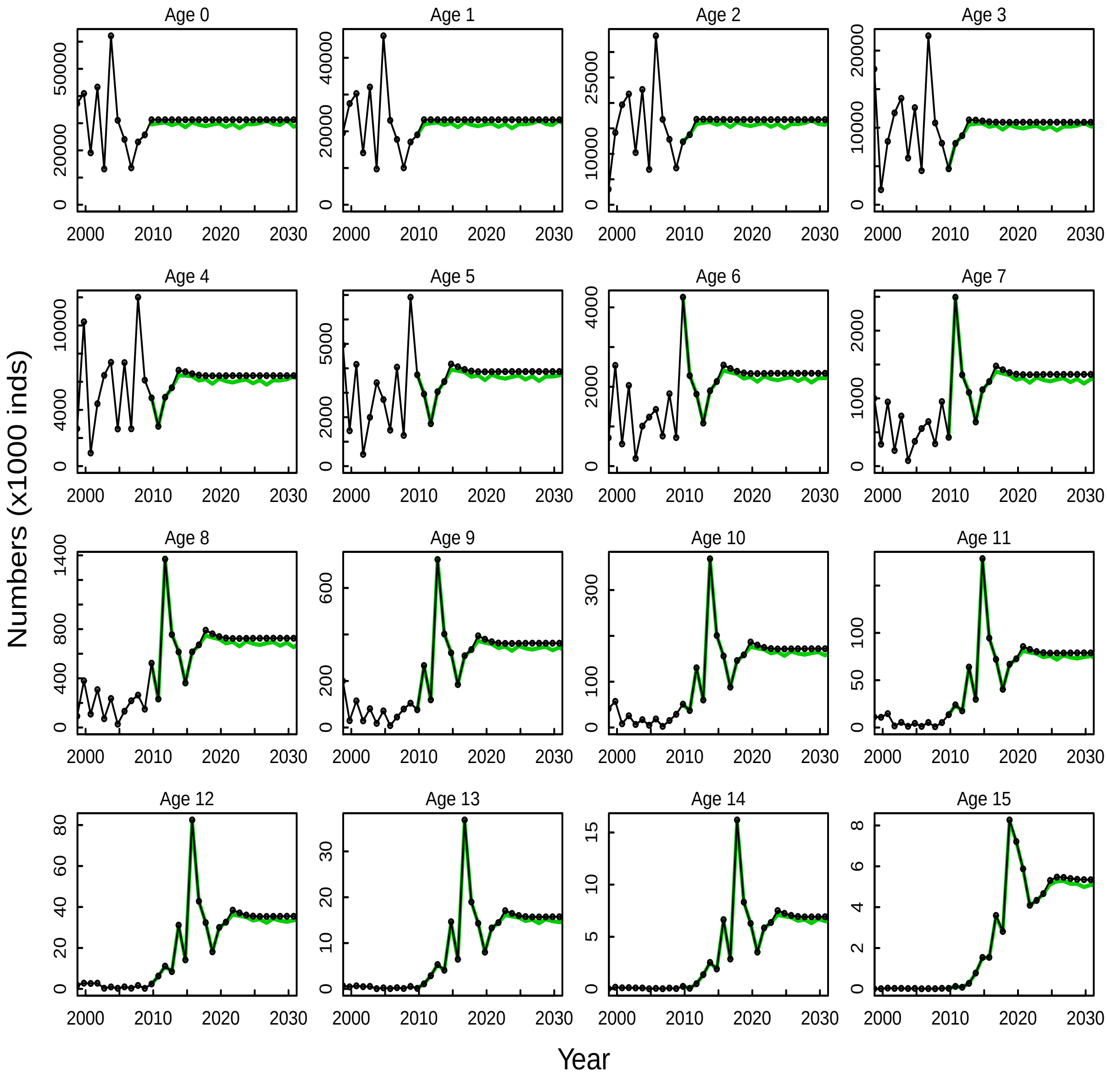

Figure 2: Comparison of numbers at age generated from stochastic projections by the R-code (average values, thick green lines) with those from a deterministic run by SS (lines with circles).

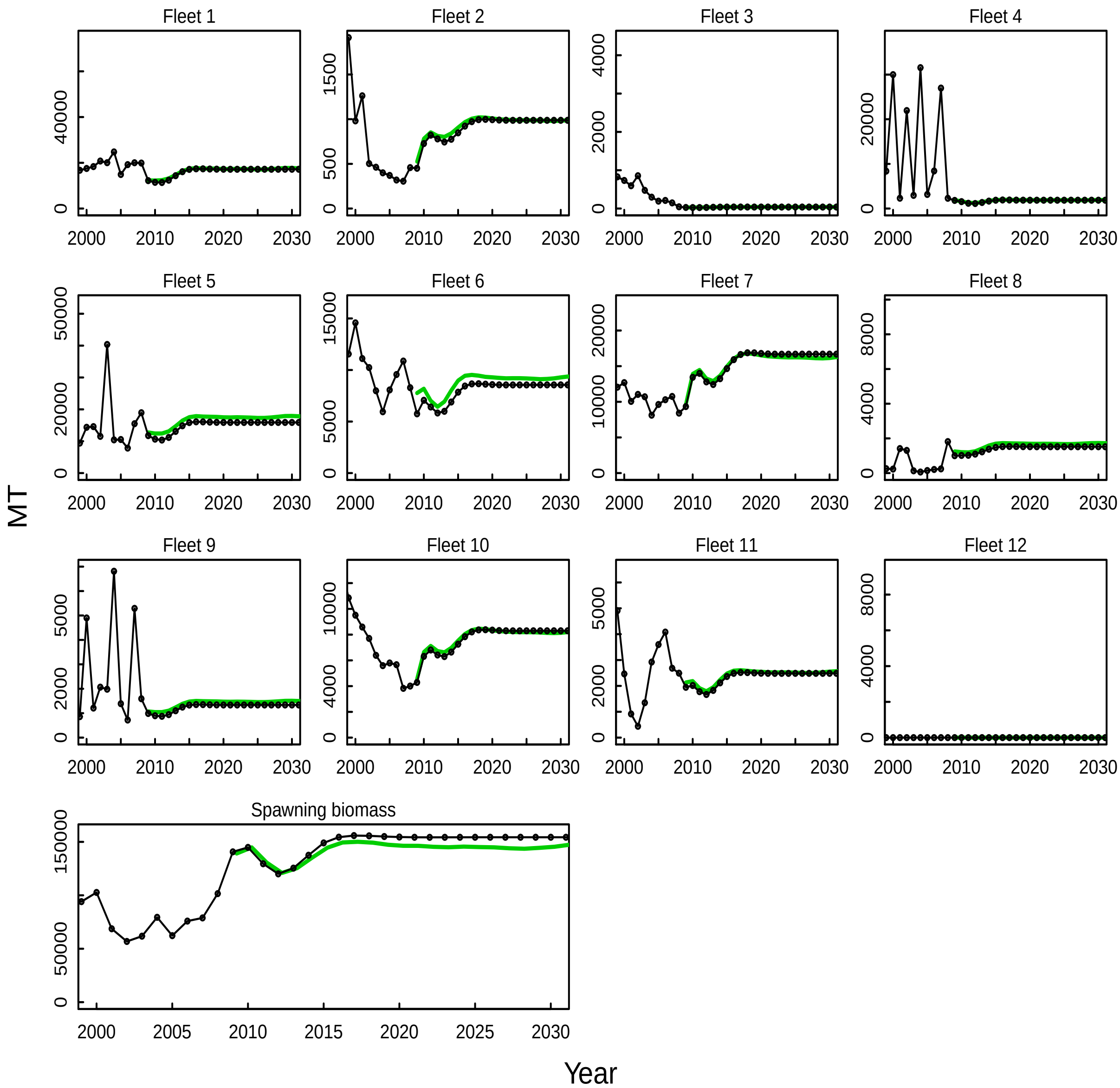

Figure 3: Comparison of catch in weight (MT) by fleets (figures titled by F1 to F12) and spawning biomass (MT) generated from stochastic projections by the R-code (thick lines) with those from a deterministic run by SS (lines with circles).